The first time I found by calculation that the square of a binocular figure was composed of the square of each of its parts, and double the product of one by the other; though convinced that my multiplication was right, I could not be satisfied till I had made and examined the figure: not but I admire algebra when applied to abstract quantities, but when used to demonstrate dimensions, I wished to see the operation, and unless explained by lines, could not rightly comprehend it.

"The Confessions of Jean Jack Rousseau" by Jean Jack Rousseau, 1789.

$$(a+b)^2 = a^2 + b^2 + 2ab \tag{1}$$

$$a^{2} = (a+1)(a-1) + 1 \tag{2}$$

$$(a+b)(a-b) = a^2 - b^2$$
(3)

$$T_n = 1 + 2 + \dots + n = \frac{n(n+1)}{2}$$
 (4)

$$T_{n-1} + T_n = n^2 (5)$$

$$1^{2} + 2^{2} + 3^{2} + \dots + n^{2} = \frac{n(n-1)(2n-1)}{6}$$
(6)

$$n^{2} = 1 + 3 + 5 + \dots + (2n - 1)$$
(7)

$$\frac{a}{b} < \frac{a+c}{b+d} < \frac{c}{d} \tag{8}$$

$$\sqrt{ab} \le \frac{a+b}{2} \tag{9}$$

$$\sin x + \cos x \le \sqrt{2} \tag{10}$$

$$F_1 = F_2 = 1, \ F_n = F_{n-1} + F_{n-2}; \ F_1^2 + F_2^2 + \dots + F_n^2 = F_n F_{n+1}$$
 (11)

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References

- 1. Mathematical Etudes. http://www.etudes.ru/en
- 2. Numberphile. http://www.numberphile.com
- 3. Roger Nelsen. http://legacy.lclark.edu/~mathsci/nelsen.html
- 4. V. I. Arnold. Continued Fractions (in Russian). http://math.ru/lib/book/pdf/mp- seria/book.14.pdf
- 5. I. M. Gelfand and A. Shen, Algebra (in Russian). http://www.mccme.ru/free- books/shen/gelfandshen-algebra.pdf